1	<i>CAGU</i> PUBLICATIONS			
1 2	Geophysical Research Letters			
3	Supporting Information for			
4	Diagnosing secular variations in retrospective ENSO seasonal forecast skill using CMIP5 model-analogs			
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11 12 13 14 15	Contents of this file Text S1 to S4 Figures S1 to S8 Tables S1 to S2			
16	Introduction			
17 18 19 20	The following gives additional details of the RMS distance metric used to choose analogs, how the trend component is included in the model-analog hindcasts, skill comparison with the NMME assimilation-initialized hindcasts, and how the CMIP5 "best-10" ensemble is chosen.			
21	Text S1.			
22 23 24 25 26 27 28 29 30	<u>The RMS distance</u> Ding et al (2018) defined a root-mean-square (RMS) distance to choose analogs. The RMS distance between a target state $\mathbf{x}(t)$ and a library state $\mathbf{y}(t')$ is given by $d^2(t,t') = \sum_{i=1}^2 \sum_{j=1}^J \left(\frac{x_j^i(t)}{\sigma_x^i} - \frac{y_j^i(t')}{\sigma_y^i}\right)^2$, with superscripts $i = 1$ indicating SSH anomalies (SSHAs) and $i = 2$ SST anomalies (SSTAs), and subscript j representing a gridpoint index with J total gridpoint indices within the training region. In the distance equation, σ_x^i and σ_y^i indicate respective area averaged standard deviations for the target and library states. Readers can refer to Ding et al (2018) for more details on the model-analog technique.			
	1			

31 **Text S2.**

- 32 The North American Multi-model Ensemble (NMME) hindcasts
- 33 We obtained retrospective forecast (hindcasts) from eight different models in the current
- 34 North American Multi-model Ensemble (NMME) project (Kirtman et al. 2014); see
- 35 Table S1 for details. To calculate anomalies, all hindcasts are "bias-corrected": the mean
- 36 hindcast drift as a function of lead and calendar month is removed separately for each
- 37 ensemble member of each model, as is common practice with CGCM seasonal forecasts
- 38 (Stockdale 1997; Saha et al. 2006; Kirtman and Min 2009). Following Barnston et al.
- 39 (2015), the grand multi-model ensemble mean (NMME grand ensemble mean) forecasts
- 40 were then determined using the bias-corrected ensemble members of all the models.

41 **Text S3.**

42 Accounting for externally-forced trends

43 First, we assume that the externally-forced component is separable from internal 44 variability; then, following the method in Dai et al. (2015), any anomaly x is

45

$$x(j,t) = x_F(j,t) + x_I(j,t)$$

46 where *j* and *t* denote grid point and time, respectively, $x_F(j, t)$ is the externally forced 47 component, and $x_I(j, t)$ is the internal climate anomaly. Suppose that T(t) represents the 48 best estimate of the evolving global mean surface temperature response to historical 49 external forcing (Dai et al., 2015). The externally-forced component is then estimated by 50 linear regression of x(j, t) onto T(t):

51

52
$$x_F(j,t) = b(j) \times T(t) ,$$

53 where b(j) is the regression slope at grid point *j* determined over the entire period. The 54 initial internal (i.e., detrended) anomaly is then the residual

55 56

$$x_{I}(j,t) = x(j,t) - b(j) \times T(t)$$

57 Note that $x_I(j, t)$ is now used to determine analogs within the fixed climate control 58 simulation, instead of x(j, t) as was done by D18. Finally, the linear estimate of the 59 externally-forced component is added back to each model-analog forecast ensemble 60 member, resulting in the final forecast ensemble $\{y(t'_1 + \tau) + b \times T(t + \tau), ..., y(t'_k + \tau) + b \times T(t + \tau), ..., y(t'_k + \tau) + b \times T(t + \tau)\}$, which is then verified against 62 $x(t + \tau)$.

63 Note that $T(t + \tau)$ is used instead of T(t), to determine externally-forced 64 contributions to the seasonal forecast. The trend clearly has a large impact on skill; for 65 example, Fig. S1 shows that the skill coming from just the predicted trend component alone is quite large for SST hindcasts (although not for precipitation) in the Indian and 66 west Pacific oceans. However, the impact of predicting the trend over the forecast lead 67 68 time is very small, as is also shown in Fig. S1, which shows that the skill due to merely 69 persisting the trend component (that is, using T(t) in the forecast instead) is almost the 70 same. That is, the primary benefit of including the trend component is to allow the initial 71 state to better match observations, especially in regions where the trend dominates natural variability. In other words, within each 1-year forecast period, the evolution of the
externally-forced trend component is slight. It is not the externally-forced trend over the
next 1-year forecast period that matters, but the external-forcing induced trend that
accumulated over the past fifty years.

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This figure then also suggests that this skill is largely due to the skill metrics that
are typically used for seasonal forecasts, so that a skill metric based on comparing
detrended anomalies with detrended hindcasts would yield much lower values in the
western Pacific and Indian ocean.

81

Anomaly correlation



82 83

84 **Figure S1.** Evaluation of external forcing as hindcasts for SST (a, c) and precip (b, d). In (a, b), time 85 evolution of $T(t + \tau)$, arising from τ , is taken into account; while in (c, d), T(t) is fixed for all lead time τ . 86 See Text S3 for details.

87

88 We determined T as the global and ensemble mean surface temperature of the CMIP5 89 multi-model historical (pre-2005) and RCP4.5 (post-2005) runs, rather than directly from 90 observations, so that the model-analog technique can make forecasts as well as hindcasts. 91 In essence, the CMIP5 ensemble mean predicts the externally-forced component, and the 92 model-analog technique predicts the internal climate anomaly. We used all 45 CMIP5 93 historical simulations to estimate the externally-forced signal, although using just those 94 models corresponding to our model-analog ensemble yielded essentially the same results. 95 For each initial state at time t, the regression coefficient b(i) was separately determined 96 from the 1961-2015 period except for data from the interval [t, t + 5 yrs], which was 97 withheld to ensure that the trend component of each hindcast was independent of the 98 verification data.

- 99
- 100 **Text S4.**

101 Choosing the "best-10" CMIP models

We note that a few models (e.g., CCSM4 and IPSL-CM5B-LR) are slightly more
 skillful than the 28-model mean in the central equatorial Pacific, perhaps because the 28-

104 model mean skill is reduced by including some models with very low skill. For example,

- 105 Table S1 shows that CMIP5 model Niño3.4 SST 6-month forecast skill ranges between
- 106 0.49-0.75. We explored the impact of adding models with less skill to the grand ensemble
- 107 mean by ordering the models based on Nino3.4 SST 6-month forecast skill, and then

108 including them one at a time in the multi-model grand ensemble mean (see Fig. S5). We

- 109 found that the multi-model mean skill reached a maximum for an ensemble size of
- between 5-12 models, but beyond this point the forecast skill degraded as models with poorer performance were added. This suggests that only a subset of the 28 models is
- 111 poorer performance were added. This suggests that only a subset of the 28 models is 112 necessary to maximize forecast skill. Several recent studies also have found that an
- ensemble including only some models, determined using some suitable criteria, may
- 114 yield higher forecast skill relative to using all available forecast models (e.g., Chen & van
- den Dool, 2017). However, note that the overall change in skill in predicting Nino3.4
- 116 SST is modest: rising from ~ 0.75 for the best model to ~ 0.775 for 5-12 models and then
- declining to only 0.73 for all 28 models (Fig. S5). As an example, in Fig. 1 we also show
- the skill of the model-analog multi-model ensemble determined from the ten most skillful
- 119 CMIP5 models from Fig. S5 (marked by stars in Table S2). This "best-10" grand
- 120 ensemble mean modestly improves skill over the 28-model mean in the tropical Pacific,
- 121 with 0.7 correlation covering a larger area, but does not much improve skill elsewhere.
- 122
- 123



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Figure S2. Skill of NMME (a,b) assimilation-initalized and (c,d) model-analog hindcasts of SST (a, c) and
precipitation (b, d) anomalies at six-month lead, for the years 1982-2009. Only anomaly correlation is
shown. Panels (a-b) show the NMME grand mean conducted by the same four models (Table S2); panels
(c-d) show the grand mean of multi-model analogs, based on the four models: CM2.1, CM2.5 FLOR,
CCSM4 and CESM1. The projected response to external radiative forcing is added to model-analog
hindcasts.

Root Mean Square Error Skill Score



134

Ranked Probability Skill Score





Figure S4. The same as Fig. S2 except for ranked probability skill score (RPSS).



138 Figure S5. The red curves show model-analog multi-model mean 6-month lead forecast skill of Nino3.4 139 SST anomalies, measured by (a) correlation and (b) RMS skill score, as a function of number of models 140 (abscissa). The 28 grand ensembles are made as follows: 1) individual model-analog ensemble mean 141 correlation skill of Nino3.4 SST is calculated at 6-month lead; 2) correlation values are ranked in 142 descending order; 3) grand model-analog ensembles are constructed by beginning with the model with 143 highest correlation, which is model 1 in abscissa and then adding one more model, with lower correlation 144 than the previous models, to the grand ensemble until all the models are added. The "best-10" grand 145 ensemble denotes 10 in abscissa. The black curves show the evaluation of individual model ensemble 146 mean, and the models are shown in the descending order in 6-month lead correlation skill of Nino3.4 SST. 147



Figure S6. Model-analog hindcast skill for Nino3.4 SST during 1961-2015, as a function of forecast lead

150 time (abscissa) and initial month (ordinate). Shading denotes correlation. Analog hindcasts are based on (a) 151 the NMME models and (b) the "best-10" CMIP5 models, respectively. In all model-analog hindcasts, the

152 projected response to external radiative forcing is included.





respectively. The units for SSH and SST are cm and Celsius, respectively.

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Model	Expanded model name	Number of ensemble members	Maximum lead month
COLA-RSMAS- CCSM4*	COLA–University of Miami–NCAR coupled model	10	12
NCAR-CESM1*	NCAR Community Earth System Model 1	10	12
GFDL-CM2pl- aer04*	Modified version of the GFDL CM2.1 coupled model	10	12
GFDL-CM2p5- FLOR*	GFDL Forecast- oriented Low Ocean Resolution version of CM2.5	24	12
CMC1-CanCM3	Canadian coupled model 1	10	12
CMC2-CanCM4	Canadian coupled model 2	10	12
NASA-GMAO- 062012	Modified version of the NASA coupled model	12	10
NCEP-CFSv2	NOAA/NCEP coupled model	24	10

Table S1. A list of the eight NMME models whose hindcast experiments were employed in the
NMME grand ensemble. The grand ensemble mean of all the eight NMME models is shown in
Figure 4. Model-analog method is applied to the four models, marked by an asterisk, in order to
compare with model-analog hindcasts with the corresponding NMME hindcasts (see Figs. S2S4).

Model name	Expanded model	Length of run	Month 6
	name	(yr)	correlation skill
		., ,	of Nino3.4 SST
ACCESS1-0	Australian	500	0.667
	Community		
	Climate and Earth		
	System Simulator		
	Coupled Model		
ACCESS1-3	Australian	500	0.569
	Community		
	Climate and Earth		
	System Simulator		
	Coupled Model		
CanESM2*	Second Generation	995	0 720
Currestviz	Canadian Earth	555	0.720
	System Model		
CCSM4*	Community	1050	0.758
0001014	Climate System	1050	0.750
	Model		
	version <i>A</i>		
	CMCC Carbon	277	0.656
CIVICC-CESIVI	Earth System	277	0.030
	Model		
	MOUEI CMCC Climata	220	0.620
	Model	550	0.029
	CMCC Climate	500	0.691
	Model with a	500	0.051
	resolved		
	Stratosphere		
CNRM-CM5*	Centre National de	850	0.688
	Recherches	000	0.000
	M et eorologiques		
	Coupled Global		
	Climate Model		
	version 5		
GEDL-CM3*	Geophysical Fluid	500	0.695
	Dynamics	500	0.055
	Laboratory		
	Climate Model		
	versions 3.0		
	Coophysical Fluid	500	0.600
	Dynamica	500	0.090
	Laboratory Earth		
	System Model		
	System Wodel		
	with Generalized		
1	Ocean Layer		

	Dynamics (GOLD)		
	component		
GEDI-ESM2M	Geophysical Fluid	500	0.687
	Dynamics		
	Laboratory Farth		
	System Model		
	with Modular		
	With Modular		
	Ocean Model 4		
	(MON4)		
	component		0.704
GISS-EZ-R*	Goddard Institute	550	0.721
	for Space Studies		
	Model E2, coupled		
	with the Russell		
	ocean model		
GISS-E2-R-CC	Goddard Institute	251	0.676
	for Space Studies		
	Model E2, coupled		
	with the Russell		
	ocean model,		
	Interactive Carbon		
	Cycle		
HadGEM2-CC	Hadley Centre	240	0.595
	Global		
	Environment		
	Model, version 2–		
	Carbon Cycle		
HadGEM2-ES	Hadlev Centre	575	0.514
	Global		
	Environment		
	Model version 2-		
	Farth System		
	Institute of	500	0 558
	Numerical	500	0.550
	Mothematics		
	Coupled Model		
	Coupled Model,		
	Version 4.0	1000	0.005
IPSL-CIVI5A-LR	L Institut Pierre-	1000	0.605
	Simon Laplace		
	Coupled Model,		
	version 5, coupled		
	with Nucleus for		
	European		
	Modelling of		
	the Ocean		
	(NEMO), low		

	resolution		
IPSL-CM5A-MR	L'Institut Pierre-	300	0.670
	Simon Laplace		
	Coupled Model,		
	version 5, coupled		
	with NEMO, mid		
	resolution		
IPSL-CM5B-LR*	L'Institut Pierre-	300	0.722
	Simon Laplace		
	Coupled Model,		
	version 5, coupled		
	with NEMO, new		
	atmospheric		
	physics low		
	resolution		
MIROC-ESM	Model for	630	0.494
	Interdisciplinary		
	Research on		
	Climate, Earth		
	System Model		
MIROC-ESM-	Model for	255	0.522
CHEM	Interdisciplinary		
	Research on		
	Climate, Earth		
	System Model, an		
	atmospheric		
	chemistry coupled		
	version		
MIROC5	Model for	670	0.587
	Interdisciplinary		
	Research on		
	Climate, version 5		
MPI-ESM-LR	Max Planck	1000	0.573
	Institute Earth		
	System		
	Model, low		
	resolution		
MPI-ESM-MR	Max Planck	1000	0.574
	Institute Earth		
	System		
	Model, medium		
	resolution		
MPI-ESM-P	Max Planck	1155	0.592
	Institute Earth		
	System		
	Model, low		

	resolution, and paleo mode		
MRI-CGCM3	Meteorological Research Institute Coupled Atmosphere– Ocean General Circulation Model, version 3	500	0.665
NorESM1-M*	Norwegian Earth System Model 1, medium resolution	500	0.694
NorESM1-ME*	Norwegian Earth System Model 1, medium resolution with capability to be fully emission driven	252	0.697

Table S2. A list of the 28 CMIP5 models whose preindustrial control simulations were employed
 as the data library for model-analogs. Models, marked by an asterisk, are employed in the "best-

185 7" grand ensemble.